

Demand Reduction in Multi-Unit Auctions: Evidence from a Sportscard Field Experiment

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Abstract

Recent auction theory suggests that multi-unit uniform-price auctions, as used by the U.S. Treasury for debt sales, produce incentives that may cause bidders to bid less than their true valuations, resulting in inefficient allocations and reduced revenue. In this paper, we present the results of a field experiment in which we auction nearly \$10,000 worth of sportscards in two-unit, two-person sealed-bid auctions. We randomize participants into uniform-price and Vickrey auction treatments, and find underbidding in the uniform-price auctions' second-unit bids, as predicted. In contrast with theoretical predictions, however, we find that individual's first-unit bids are significantly higher in the uniform-price than in the Vickrey treatment. The bid differences are large enough to affect the allocation of goods, as split allocations result significantly more often in the uniform-price treatment. We find no significant difference in revenues across auction formats.

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Recent auction theory suggests that multi-unit uniform-price auctions, as used by the U.S. Treasury for debt sales, produce incentives that may cause bidders to bid less than their true valuations, resulting in inefficient allocations and reduced revenue. In this paper, we present the results of a field experiment in which we auction nearly \$10,000 worth of sportscards in two-unit, two-person sealed-bid auctions. We randomize participants into uniform-price and Vickrey auction treatments, and find underbidding in the uniform-price auctions' second-unit bids, as predicted. In contrast with theoretical predictions, however, we find that individuals' first-unit bids are significantly higher in the uniform-price than in the Vickrey treatment. The bid differences are large enough to affect the allocation of goods, as split allocations result significantly more often in the uniform-price treatment. We find no significant difference in revenues across auction formats.

Nearly four decades ago, William Vickrey (1961) illustrated the appealing features of second-price sealed-bid auctions. In particular, he showed that second-price auctions induce "truthtelling" for bidders with independent private values (IPV); it is a dominant strategy for each bidder to reveal his maximum willingness to pay for the good. Hence, second-price auctions are allocatively efficient, as the bidder with the highest value always wins. In the same paper, Vickrey also considered the problem of a multi-unit auction for m units of a good. He demonstrated that full demand revelation will occur in a sealed-bid auction where each bidder submits one bid, the top m bidders each win one good at a uniform price equal to the first bid rejected. He writes, "only in this way is it possible to insure that each bidder will be motivated to put in a bid at the full value of the article to himself, thus assuring an optimum allocation of resources." A

number of economists used similar intuition when recommending the uniform-price sealed-bid format for its use in settings such as Treasury auctions.¹

As Lawrence M. Ausubel and Peter C. Cramton (1999) point out, Vickrey's caveat in his very next paragraph went unnoticed by many economists: "It is important to realize, however, that this result applies only to cases where each bidder is interested in at most a single unit... As soon as we consider the more general case where an individual bidder may be interested in securing two or more of the units, where the number of bidders is still too few to produce a fully competitive market, the possibility [of a] Pareto-optimal result... disappears." Vickrey did not find a solution to the problem of a demand-revealing auction with multi-unit bidders, but Theodore Groves (1973) and Edward H. Clarke (1971) later provided general principles for revelation mechanisms, and these principles can be applied to derive the correct multi-unit generalization for the Vickrey auction. Specifically, the rules for an m -object Vickrey auction are that bidders can submit as many individual-unit bids as they like, that the top m bids will be declared winners, and that for the k th unit won by a bidder, she must pay an amount equal to the k th highest of the rejected bids submitted by others.² When each bidder has demand for only a single unit of the good, this mechanism reduces to a uniform-price auction.

Several authors have recently investigated equilibria in uniform-price auctions with multi-unit demand, including Charles Noussair (1995), Brett E. Katzman (1995), Richard Engelbrecht-Wiggans and Charles M. Kahn (1998), and Ausubel and Cramton.

¹ For more details on recommendations of uniform-price auctions by economists, see Ausubel and Cramton (1999).

² Technically, these rules are demand-revealing only in cases where every bidder's demand curve is either flat or downward-sloping, as is assumed in the theoretical papers cited here. If bidders might have upward-sloping demands (increasing returns to scale in purchases), then this simple price rule no longer works; a slightly more complicated set of instructions would be required to implement a Groves-Clarke truth-telling mechanism.

The first three consider situations where each bidder has private values for up to two units of the auctioned good, and give examples where the predicted equilibrium involves demand reduction—second unit bids are lower than true valuations. Engelbrecht-Wiggans and Kahn provide a general characterization of equilibria in such environments. They show that bidders have a dominant strategy of truth-telling on the first unit of the good, and of demand reduction (at least weakly) on the second unit. Demand reduction is strictly greater than zero in many circumstances, including the case where both bidders' valuations are drawn independently from the same distribution. They also provide necessary conditions for the existence of “single unit bid” equilibria, where each bidder submits a bid of zero on the second unit; in the extreme, such equilibria can result in zero revenues for the auctioneer.

Ausubel and Cramton present a general theory of demand reduction and inefficiency in multi-unit auctions. They generalize previous multi-unit demand models by allowing each individual to demand an arbitrary number of units and by allowing valuations to be correlated. To simplify the analysis, they assume that the auctioned good is infinitely divisible rather than discrete. Ausubel and Cramton provide sufficient conditions for demand reduction (and hence inefficiency)³ in a uniform-price auction: as long as at least one bidder has downward-sloping demand, any Nash equilibrium is guaranteed to have bid reduction. They also show that the revenue ranking of Vickrey and uniform-price is ambiguous, depending on the underlying distribution of valuations. For most “standard” IPV probability distributions (those with a nondecreasing hazard

³ Allocative inefficiency results from demand reduction because high-value bidders who reduce their bids below their valuations potentially are outbid by bidders with lower valuations. For example, a bidder with high values on both first and second units will often win the first unit but lose the second unit to a bidder whose second-unit valuation is lower.

rates, such as the uniform), however, they predict the Vickrey auction should revenue-dominate the uniform-price auction.

Our work compares the multi-unit Vickrey format to the uniform-price format in a field experiment, contributing to the empirical literature on multi-unit auctions. Several laboratory experiments have investigated multi-unit auctions with single-unit demand, where demand reduction is not an issue (James C. Cox *et al.* (1984, 1985), Kevin A. McCabe *et al.* (1990, 1991)). Paul Alsemgeest *et al.* (1998) find some demand reduction in the laboratory, in a dynamic ascending version of a uniform-price auction whose equilibrium is unknown. Ausubel and Cramton argue that the simultaneous-ascending FCC auction format is strategically similar to a uniform-price sealed-bid auction, and present field data from the FCC spectrum auctions which are suggestive of demand reduction. Catherine D. Wolfram (1998) analyzes data from uniform-price auctions for electricity supply in England and Wales, finding evidence of the strategic behavior predicted by theory. The generators' marginal bids overstated their true marginal costs, an effect analogous to "demand reduction" in a supply auction.⁴

Our study complements the closely related paper by John H. Kagel and Dan Levin (1999). Their laboratory experiment looked for demand reduction by comparing the uniform-price sealed-bid format with Ausubel's (1997) ascending-bid version of the Vickrey auction. The experiment was carefully designed to satisfy Ausubel and Cramton's sufficient conditions for demand reduction: a single two-unit human bidder

⁴ Other multi-unit studies include Gary J. Miller and Charles R. Plott (1985), who focus on revenue comparisons between uniform-price and discriminatory auctions in the laboratory. Rafael Tenorio (1993) and Steven R. Umlauf (1993) perform similar revenue comparisons with field data on Zambian currency auctions and Mexican treasury-bill auctions, respectively. Some recent laboratory experiments have explored auction environments with subjects selling multiple units of dissimilar goods (List and Shogren (1998b)) and buying multiple units of dissimilar, complementary goods (John O. Ledyard *et al.* (1997), Charles R. Plott (1997), Mark Isaac and Duncan James (1999), David Brenner and John Morgan (1997)).

competed against robot bidders with unit demand (thus, the robots' demands were downward sloping). Confirming the theory, Kagel and Levin observed systematic bid reduction by human subjects on their second units in uniform-price auctions, by comparison both with actual values and with strategies observed in the Vickrey/Ausubel auction. However, they also observed overbidding relative to the dominant strategy on both units in the uniform-price sealed-bid auction, an effect unpredicted by theory but common to other sealed-bid laboratory studies.⁵ A third treatment, an ascending-bid implementation of the uniform-price auction, eliminated the sealed-bid overbidding effect and produced more striking demand reduction. Kagel and Levin find that although efficiency is higher in the Vickrey/Ausubel auction than in the uniform-price sealed-bid auction, revenues are higher in the uniform-price sealed-bid auction.

Our experiment differs from that of Kagel and Levin in four important ways. First, we test the uniform-price sealed-bid auction against the Vickrey sealed-bid auction, while Kagel and Levin run the dynamic (Ausubel) version of the Vickrey auction. Second, we have two human bidders per auction, rather than a single human versus a robot. Third, we use real goods rather than induced values. Fourth, we perform the experiment in the field rather than in the laboratory.

Our field experiments are most similar in methodology to those of John A. List and Jason F. Shogren (1998a) and List *et al.* (1998), who use card-show experiments to investigate questions of contingent valuation. Field experiments present a tradeoff: they give up some of the controls of a laboratory experiment (such as induced valuations, or robots guaranteed to play equilibrium strategies against human subjects) in exchange for

⁵ See, for example, Cox *et al.* (1985), Kagel *et al.* (1987), and Kagel and Levin (1993). Remarkably, Kagel and Levin (1999) still found this effect despite specifically instructing subjects that overbidding valuations

increased realism.⁶ Our experiments match the real-world settings which auction theory attempts to explain: our bidders compete for real goods rather than explicit cash values, they are not told explicitly the distributions of other's valuations, and they are likely to have previous experience bidding for the types of goods being auctioned.⁷ Field experiments provide a useful middle ground between the tight controls of the laboratory and the vagaries of completely uncontrolled field data.

I. Experimental Design

We designed our experiment to compare outcomes in uniform-price and Vickrey sealed-bid auctions, with particular attention to the question of demand reduction. We conducted equal numbers of Vickrey and uniform-price auctions, with different bidders in each auction. We also experimented with bidder type, conducting some of our experiments with professional card dealers and others with nondealers. This treatment was designed to capture the distinction between the theoretical cases of bidders with steep downward-sloping demands (individual consumers) and those with relatively flat demands (dealers) for multiple identical units. The auctioned sportscards fit into two price categories: low (book value of \$3) and high (book value of \$70). We conducted our treatments in June, 1998, at a sportscard show in Orlando, FL, where we had a ready supply of card collectors interested in bidding in the auctions.

could never increase profits, only reduce them.

⁶ Lucking-Reiley (1999a, 1999b) gives up even more control in his field experiments, using Internet-based auctions in a preexisting market with an unknown number of participating bidders. These papers test the theory of reserve prices in first-price sealed-bid auctions, and the theory of revenue equivalence between the four different single-unit auction formats.

⁷ Given the proliferation of sportscard auctions, we feel we can safely assume that most of our participants (all recruited at a sportscard trade show) have previous experience bidding in auctions for such goods. For example, see *Sports Collectors' Digest*, a weekly publication filled with sportscard and sports memorabilia auctions.

For the low-priced card auctions we chose a Joe Montana 1982 *Topps* football card and a 1989 Michael Jordan *Hoops* basketball card. Both cards had a June 1998 book value of \$3. For the higher-priced auctions we selected a Cal Ripken, Jr. 1982 *Topps* baseball card and a Barry Sanders 1989 *Score* football card. These two cards had book values of approximately \$70. We sold dozens of each type of card, with all the cards in identical condition. All lower priced cards were independently graded by a sportscard dealer as “near-mint”, and each higher-priced card was graded as “PSA 8 near-mint” by a well-known agency, Professional Sports Authenticators (PSA).⁸ All auctions for a given card type displayed the same sportscards to bidders, and identical copies were sold to winning bidders after the auctions concluded.

For the simplest possible test of demand-reduction theory, we chose a design with two bidders and two goods per auction. We invited two bidders to submit two bids each for two identical sportscards, in an auction with no reserve price. We chose the auction format and card type for each subject according to a prespecified plan, to avoid accidentally introducing experimenter bias. After receiving bids from subjects within a given treatment, we randomly matched pairs of bidders to determine the outcome of each two-person auction. No participant bid in more than one auction. Our design is intended for between-subject comparisons; we draw our subjects from the same population, and test whether the auction treatment has statistically significant effects on the average behavior of the population.⁹

⁸ Since PSA charges a grading fee of \$10 per card, we chose not to have the \$3 cards graded by PSA.

⁹ Ideally, we would obtain data on a single subject bidding on the same card type in the two different auction formats, in order to do within-subject comparisons. However, doing the two auctions in sequence would most likely have changed bidders’ demands for the goods (as two cards would already have been awarded by the time the second auction took place), thus destroying the ability to compare the two auction formats while holding all else equal. We considered collecting bids in both treatments from the same subject and randomizing which auction would actually “count” towards a real transaction, but rejected this

Each participant's experience followed four steps: (1) inspection of the good, (2) learning the auction rules, (3) placing two bids, and (4) conclusion of the transaction. In Step 1, a potential subject approached the experimenter's table and inquired about the sale of the two sportscards displayed on the table. The experimenter then invited the potential subject to take about five minutes to participate in an auction for the two sportscards. If the individual agreed to participate, he could pick up and visually examine each card (in a sealed cardholder, with the graded card condition clearly marked). The experimenter worked one-on-one with the participant, and imposed no time limit on his inspection of the cards.

In Step 2, the administrator gave the participant an instruction sheet that consisted of two parts: (1) an auction rules sheet which also included a practice worksheet, and (2) a bidding sheet.¹⁰ In each auction type we informed the bidders that card dealers would bid against one other card dealer, and nondealers would bid against one other nondealer. We changed the auction format and card type at the top of each hour, so subjects were assigned to each treatment based on the time they visited our table. The instruction sheets were identical across treatments, except for the explanations of the pricing rules.

In the uniform-price treatment, subjects read that "For each card won, the purchase price is equal to the amount of the third-highest bid (that is, the highest losing bid)," and they saw an example with bids ranked and labeled \$A, \$B, \$C, and \$D. In the Vickrey treatment, subjects read that "For each card won, the purchase price will be determined as follows. For the first unit you win, you pay an amount equal to the highest rejected bid which was not your own. For the second unit you win, you pay an amount

idea in favor of keeping the environment as simple and realistic as possible. By explaining only one format to each bidder, we felt we would reduce the possibility of confusion.

equal to the second-highest rejected bid which was not your own.” Because this rule is relatively complicated, they saw three different examples to illustrate possible outcomes with bids labeled \$A, \$B, \$C, and \$D. We avoided using actual dollar amounts in the examples, in order to avoid anchoring of bids.

After reading the auction rules, each participant worked through a bidding worksheet where she was asked to make up two numeric bids for each of two bidders, then to compute the final allocation and prices paid. The experimenter checked the participant’s answers to ensure that the subject understood the auction rules. After having her questions answered, the participant placed her two official bids on the bidding sheets (Step 3).¹¹

Finally, in Step 4 the experimenter explained that the bidder should return at a specified time (within several hours) to find out the results of the auction and conduct any resulting transactions. Transactions took place at 1PM and 5PM both Saturday and Sunday. If a winning bidder did not return for the specified transaction time, she would be contacted by phone within three days after the show in order to complete the transaction. Upon receipt of payment, we would pay the postage required to send the card(s) in the mail to the winning bidder.

The dealer treatments took place in the same way as the non-dealer treatments, with one exception. Instead of waiting for participants to arrive at the auction booth, the experimenter visited each dealer at his/her booth before the sportscard show opened,

¹⁰ Verbatim copies of the experimental instructions are available in the Appendix.

¹¹ In laboratory experiments, more than one trial is often required before people understand the nature of certain auction mechanisms. We decided to use a one-shot auction so we could run the experiment on the floor of the sportscard show. To test whether subjects understood the auction mechanism, we ran a pilot study in May 1998 at a similar sportscard show in Orlando. On completion of these hypothetical auctions, subjects answered questions about their understanding of the auction rules. Approximately fifteen people took part in each auction type, and no one had any problem understanding the allocation and price rules.

alternating the auction format and card type. The non-dealer treatments took approximately fifteen hours to complete (9:30am to 5pm on Saturday and Sunday), while the dealer treatments took only two-and-a-half hours (7:00am to 9:30am on Saturday).¹²

Table 1 shows the number of auctions of each type in our experimental design. In total, we ran 164 different two-unit auctions, including 82 uniform-price and 82 Vickrey. We auctioned 328 sportscards with a total book value of nearly \$10,000.

(Table 1 near here)

II. Results

We test several predictions of the theory of demand reduction discussed above. First, we expect to observe lower second-unit bids in the uniform-price auction compared to the Vickrey auction.¹³ Second, we expect no difference between first-unit bids in the uniform-price auction and those in the Vickrey auction. Third, we expect to find more zero bids in the uniform-price treatment than in the Vickrey treatment.¹⁴ Finally, we expect revenues to be lower in the uniform-price auction than in the Vickrey auction.¹⁵

Table 2 reports summary statistics for our auction data. The first four columns of Panel A display means and standard deviations of the bids submitted in each auction type. One pattern in the data is that first-unit bids are larger in the uniform-price auctions

¹² The dealer sessions were completed in a more timely fashion because the dealers (in their booths setting up their own cards) were more accessible, and they understood the auction rules more quickly than the nondealers (a number of the dealers actually run auctions themselves). To discourage collusion and/or information asymmetries, we swore each of the dealers to secrecy about our cards and auction formats. (Collusion was unlikely to be a factor anyway, with 100 dealers and over 200 nondealers matched randomly in pairs in our experiments.)

¹³ Demand reduction is not guaranteed by Ausubel and Cramton's inefficiency theorem in our experiments; it is difficult to guarantee in an auction for real goods that at least one bidder has downward-sloping demand. However, the existence (if not uniqueness) of demand-reduction equilibria is predicted by the theory, and our study aims to detect whether this is a measurable effect.

¹⁴ Engelbrecht-Wiggans and Kahn note, "we may observe fewer bids in such uniform-price auctions than in other forms of multi-unit auctions, a potentially testable implication." To our knowledge, this is the first study to test that hypothesis.

than in the corresponding Vickrey auctions. The magnitude of the difference is around \$10 for the high-priced (\$70) cards, and \$0.03 to \$0.46 for the low-priced (\$3) cards. The ranking reverses for second-unit bids, supporting demand reduction theories: Vickrey second-unit bids are approximately \$12 higher than the corresponding uniform-price bids for high-priced cards, and \$0.05 to \$0.30 higher for the low-priced cards. Further evidence of demand reduction is contained in the next two columns of Panel A, which present differences between first and second bids—a measure of the steepness of each bidder’s downward-sloping bid schedule. In each treatment, the mean difference between first-unit and second-unit bids is much larger in the uniform-price than in the Vickrey auctions.¹⁶

(Table 2 near here)

The rightmost columns of Panel A in Table 2 give descriptive statistics for auction revenues generated by each pair of cards. Mean revenues ranged from as low as 11% of book value (in nondealer auctions for low-priced cards) to as high as 54% of book value (in dealer auctions for high-priced cards); low revenues are unsurprising in auctions where only two randomly-selected bidders competed for two cards.¹⁷ Dealer auctions had higher ratios of revenue to book value than did nondealer auctions; this

¹⁵ As noted above, this prediction is not guaranteed by the theory, but it is true for the standard distributions used to provide concrete examples in auction theory.

¹⁶ For example, differences between bid one and bid two were \$7-\$23 in the Vickrey auctions for expensive cards, compared with \$30-\$45 in the uniform-price auctions. For the lower priced cards, bids differed by \$0.80-\$0.90 in the Vickrey auctions, and \$1.00-\$1.50 in the uniform-price auctions.

¹⁷ To the extent that revenues are lower than could have been earned through another selling mechanism, this represents personal financial investment in the research by the experimenters. We could have invited more bidders to increase revenues and thereby save money, but we felt that a two-bidder environment gave us the best chance to observe demand reduction. Similarly, we might have used positive reserve prices to avoid selling cards at very low prices, but this would also have reduced our ability to observe demand reduction (by reducing the number of observed bids and narrowing the range of acceptable bids).

probably indicates that nondealers tend to have lower demand schedules for the auctioned cards. There seems to be no systematic difference in revenues across auction formats.

We next present formal statistical tests of our hypotheses. The second panel of Table 2 contains t-statistics and two-tailed p-values for each of the hypotheses discussed below.¹⁸

II. A. First-Unit and Second-Unit Bids

One way to test for demand reduction is to examine first-unit bids and second-unit bids individually. Theory predicts that first-unit bids should be equal on average in the two auction formats since both auctions have the same dominant strategy for first-unit bids, and that second-unit bids should be lower on average in the uniform-price format through strategic demand reduction. Because we are most interested in the presence of strategic demand reduction, we first examine second-unit bids. The corresponding column of Panel B in Table 2 shows that all five t-statistics have the expected positive sign, indicating that second bids were larger in the Vickrey auctions. The p-values indicate that this difference is statistically significant for the high-value (\$70) cards ($p = 0.005, 0.001$), but not for the low-value (\$3) cards ($p = 0.638, 0.235, 0.733$).

The results on first-unit bids, in the first column of Panel B in the table, also provide interesting insights. Despite the theoretical prediction of equality of first unit bids across auction types, our point estimates show that first unit bids are higher on average in the uniform-price auctions, and this is robust across all five treatments. These effects are similar in magnitude to the second-unit bid reduction found above, but are

¹⁸ We report results of a large-sample test, which does not require stringent assumptions about the exact shapes of the underlying distributions in order to generate a normally distributed test statistic. The large-sample assumption may be somewhat strained for our smallest pair of samples (only 20 observations per sample). As a robustness check, we also conducted small-sample t-tests that assume the populations have normal distributions and equal variances, and the results were not qualitatively different in any of the tests.

opposite in sign. Formal tests again indicate statistical significance for the \$70 cards ($p = 0.077, 0.002$), but not for the \$3 cards ($p = .706, .377, .937$). We find the presence, not to mention the magnitude, of this effect quite surprising, as it is not predicted by any theory of which we are aware. Because we cannot observe valuations directly, this difference in first-unit bids could represent either overbidding in the uniform-price auction and/or underbidding in the Vickrey auction.

II. B. Bid Schedules

The previous subsection's evidence of demand reduction uses information on individuals' first and second-unit bids. We can perform a potentially more powerful test of demand reduction by analyzing an individual's entire demand schedule. That is, we compute the difference between an individual's first-unit bid and his second-unit bid, and test whether the mean difference varies across auction treatments. Demand-reduction theory predicts that the mean difference will be greater in the uniform-price treatment, since first-unit bids should be unaffected across treatments while second-unit bids should be reduced in the uniform-price auction.

The third column in Panel B of Table 2 presents the results of this hypothesis test. For the high-value card treatments, bid differences are statistically significant ($p < 0.001$), as predicted. For each of the two low-value cards auctioned to nondealers the differences have the predicted sign but are statistically insignificant ($p = 0.391$; $p = 0.800$). The evidence is stronger in the dealer treatment for the low-value card ($p = 0.128$), suggesting that dealers exhibit some demand reduction on the low-value cards as well as on the high-value cards. By contrast, the nondealers appear to exhibit demand reduction only on the high-value cards.

The bid-reduction effect appears to be more prominent when the stakes are higher. In light of recent research on decisionmaking in the presence of cognitive costs, this finding is intuitively appealing.¹⁹ The results also suggest that with low-priced cards, dealers may be more likely to bid strategically, perhaps because they have to exert less effort to formulate optimal bidding strategies as dealers most likely have more experience with auctions. Though several laboratory experiments have investigated the effects of the size of stakes, we believe ours is the first study to document a similar effect in the field.

A related test examines the proportion of flat bid schedules. Some bidders might value the second unit of a card just as much as the first one; we expect this to be particularly true for dealers, who can often resell the second unit of a card just as easily as the first. If such a bidder truthfully reveals her demand, we would expect her bid schedule to be completely flat (zero difference between first-unit and second-unit bids). The fifth and sixth columns of Table 3 report the proportion of bidders who submitted flat bid schedules.

Demand-reduction theory predicts that the proportion of flat bid schedules should be lower in the uniform-price auction than in the Vickrey auction. Pooling across treatments since this test does not rely on bid magnitudes, we find sample proportions of 23/164 (14%) and 45/164 (27.4%) for the uniform and Vickrey auctions. A test of the null hypothesis of equality yields a p-value of 0.003, indicating that the uniform-price auction yields significantly fewer flat bid schedules across the combined set of five treatments, as predicted.

¹⁹ See Vernon L. Smith and James M. Walker (1993) for an example of such a theory, and its application to experimental evidence. Robert Slonim and Alvin E. Roth (1998) present a recent example of higher stakes causing behavior to become more consistent with Nash equilibrium. John Conlisk (1996) provides a nice review of research on the topic of decisionmaking with deliberation costs.

(Table 3 near here)

II. C. Zero Bids

How extreme is the amount of demand reduction in our uniform-price auctions? As noted earlier, Engelbrecht-Wiggans and Kahn (1998) predict that a higher proportion of second-unit bids will equal zero in uniform-price auctions than in Vickrey auctions. This is strong demand reduction, a second-unit bid reducing all the way to zero. First-unit bids should be unaffected; the choice of auction format should cause more zeros only on second-unit bids. Columns 1-4 of Table 3 provide data on the number of bids equal to zero in each of the auction treatments. Since bid magnitudes do not matter in these tests, we pool data across card types. For first-unit bids, we received 9 zeros out of 164 bids (5.5%) in the Vickrey treatment, and 6/164 (3.7%) in the uniform-price treatment. A formal statistical test indicates no significant difference between these proportions ($z = 0.79$, two-tailed $p = 0.428$), which is consistent with the theoretical prediction. All 15 of the zeros received in first-unit bids occurred in the nondealer treatments with \$3 cards; this most likely indicates that those 15 individuals literally had zero demand for the cards.²⁰

The more important test is that for second-unit bids. Here we see 33 of 164 bids (20.1%) equalling zero in the Vickrey treatment, compared with 43 of 164 (26.2%) in the uniform-price treatment. This difference is not statistically significant at conventional levels ($z = -1.31$, $p = 0.191$). However, given our earlier results that suggest low stakes do not induce strategic behavior among nondealers, we chose to redo this test excluding

²⁰ Given the earlier results on lack of demand reduction in the low-value nondealer treatments, this finding could also be a reflection of reduced rationality by nondealers in bidding for low-value cards.

the Montana and Jordan nondealer treatments.²¹ For the pooled data on the other three treatments, a formal test shows that the proportion of zero bids is significantly higher in the uniform-price auction format ($z = -3.22$, $p = 0.001$). Thus, at least in the treatments with high stakes or more experienced bidders, we find evidence of more zero bids in the uniform-price auction format, a result predicted by theory.

II. D. Allocation of Goods

Demand reduction matters most when it causes allocative inefficiency, moving the equilibrium allocation of goods away from the Pareto optimum. Despite the clear statistical evidence of demand reduction in this study, the allocation effects might still be inconsequential. Demand-reduction theory predicts a single type of distortion from efficiency in a two-bidder, two-good uniform-price auction: a bidder with high values for both units reduces his bid so much on the second unit that a second bidder with strictly lower values manages to win one of the two goods. This split allocation of goods produces lower total surplus than would an allocation that gives both units to the high-value bidder.

Because this is a field experiment, we do not observe bidders' true valuations for the goods, and therefore we cannot provide a direct test of inefficiency. We can, however, observe whether allocations appear to be significantly different between the two auction formats: do uniform-price auctions result in more split allocations of the two goods than Vickrey auctions? The data in the final two columns of Table 3 address this question.

With the exception of the dealer treatment for Joe Montana (\$3) cards, in every treatment the sample proportion of split allocations is higher for the uniform-price

²¹ Note that this automatically excludes all observations with first-unit bids equal to zero.

auction than for the Vickrey auction. In total, 34 of 82 auctions (41.5%) produced split allocations in the Vickrey treatment, compared with 53.5²² of 82 auctions (65.2%) in the uniform-price treatment. The pooled data allow us to reject the null hypothesis of equality between those proportions ($z = -5.31$ $p < 0.001$). Thus, the proportion of split allocations is significantly higher in uniform-price auctions than in Vickrey auctions. We conclude that demand reduction is large enough to have economically significant effects on allocative efficiency.

II. E. Revenues

Another natural question to ask is which auction format produces greater revenues. As noted earlier, the theoretical literature yields uncertain revenue rankings of the two auction formats, depending on the underlying structure of bidder demands, but the simplest examples tend to produce lower revenues in the uniform-price auction.²³ Data on revenues are in the rightmost columns in Panel A of Table 2, while results of hypothesis tests for each treatment can be found in Panel B of Table 2. The rankings are indeed ambiguous: two of the treatments produced higher mean Vickrey revenues, while three produced higher mean uniform-price revenues. In none of the cases was the revenue difference statistically significant.²⁴

Kagel and Levin (1997) find that uniform-price auctions revenue-dominate ascending-format Vickrey auctions, in a demand environment where the clear theoretical prediction was for the Vickrey auction to dominate. By contrast, we find that the

²² Some auctions were ambiguous in their allocation, because they had ties for the second-highest bid in the auction. In practice, we flipped a coin to determine the winner. For statistical purposes, we chose to classify such outcomes as 0.5 of a split allocation, since such outcomes were equally likely to result in splits as in two-unit packages.

²³ Extreme examples include the zero-bid equilibria of Engelbrecht-Wiggans and Kahn, where revenues are positive in the Vickrey auction but zero in the uniform-price auction.

uniform-price and Vickrey auctions cannot be revenue-ranked. This could be due to the difference between the laboratory and the field: demand conditions are known and regular in the laboratory, but unknown and potentially variable in the field. Indeed, Ausubel and Cramton show that the revenue rankings can depend critically on the underlying demand structure. Alternatively, the difference between our findings and those of Kagel and Levin could be due to the fact that our Vickrey auctions were sealed-bid while theirs were ascending. Their results indicate that sealed-bid auctions generate overbidding relative to ascending auctions in general, so our comparison of two sealed-bid formats could have eliminated their revenue differences. We conclude that, at least for sportscard auctions, Vickrey sealed-bid auctions may be substituted for uniform-price auctions without an appreciable loss of revenue.

III. Concluding Remarks

Multi-unit auctions with multi-unit demand are extremely important in practice, from Treasury bill auctions to FCC spectrum auctions to commercial Internet auctions for computer equipment and other goods. A recent wave of auction theory has begun to model multi-unit auctions in more detail, and in this paper we conduct empirical tests of this new body of multi-unit auction theory. By running field auctions for sportscards using both the Vickrey and the uniform-price sealed-bid auction formats, we test the theoretical prediction that demand reduction is an important factor in uniform-price auctions.

Our data yield several important findings. First, demand reduction is evident in the uniform-price auctions, relative to the Vickrey auctions. Second, the amount of

²⁴ Our revenue results are likely to be due in part to the two countervailing bid effects we found: first-unit bids favor the uniform-price auction, while second-unit bids favor the Vickrey auction.

demand reduction is frequently large: the uniform-price auction results in significantly more bids of zero, and the bid reductions are large enough to cause frequent changes in the allocation of goods.²⁵ Third, we find an anomalous result that does not conform to theoretical predictions: first-unit bids are higher in uniform-price auctions than in Vickrey auctions. Fourth, revenues are not systematically different across auction formats, so efficiency gains in the Vickrey auction do not come at the expense of reduced revenues for the seller.

We hope to see these results replicated and extended to more complicated environments. First, one could replicate the same experiments with induced values, in order to establish a more direct connection between the laboratory and the field. Second, one could consider increased numbers of bidders and goods, since multi-unit auctions typically involve more than two bidders and more than two goods. Increased numbers of bidders might reduce demand-reduction effects, by decreasing the probability of one's own bid affecting the price. Increased numbers of goods might have the opposite effect, as the possibility of more units at a lower price could increase the incentives for demand reduction. We anticipate that future theoretical and empirical work will address these issues.

²⁵ Our finding of demand reduction has potentially broad implications. In addition to the well publicized auctions for Treasury debt sales and communications spectrum rights, we note that WR Hambrecht+Co has recently announced uniform-price auctions for initial public offerings of corporate shares through its OpenIPO Web site. Our results may also be relevant to auctions for pollution emission permits, especially in thin regional markets (see Timothy Cason and Charles Plott (1996) and Robert Godby (1998)).

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Table 1. Experimental design.

Card	Book Value	Non-Dealers ^a		Dealers ^a	
		Uniform	Vickrey	Uniform	Vickrey
Barry Sanders 1989 <i>Score</i>	\$70	17	17	---	---
Cal Ripken, Jr. 1982 <i>Topps</i>	\$70	---	---	15	15
Michael Jordan 1989 <i>Hoops</i>	\$3	25	25	---	---
Joe Montana 1982 <i>Topps</i>	\$3	15	15	10	10

^a Each auction had two invited bidders who submitted up to two bids each. The numbers in the cells represent the number of auctions run for each treatment type. For example, with 1989 *Score* Barry Sanders cards we ran 17 uniform-price auctions and 17 Vickrey auctions, with two cards each, for a total of 68 Barry Sanders cards sold.

Table 2. Bids and revenues.

Panel A: Descriptive statistics.^a

	Bid #1 ^b		Bid #2 ^c		Bid#1-Bid#2 ^d		Revenue ^e	
	Vickrey	Uniform	Vickrey	Uniform	Vickrey	Uniform	Vickrey	Uniform
Sanders (ND) ^f	\$51.82 (23.44)	\$62.35 (25.67)	\$28.82 (19.98)	\$16.62 (15.40)	\$23.00 (19.68)	\$45.74 (25.71)	\$51.06 (34.03)	\$48.71 (32.26)
Ripken (D)	49.60 (15.19)	62.67 (15.28)	41.77 (14.46)	30.60 (13.43)	7.83 (9.16)	32.07 (20.13)	72.87 (25.26)	76.13 (21.31)
Jordan (ND)	1.73 (1.51)	1.83 (1.35)	0.91 (1.04)	0.82 (0.85)	0.82 (1.11)	1.02 (1.18)	1.13 (1.52)	1.71 (1.34)
Montana (D)	2.03 (0.86)	2.49 (2.18)	1.26 (0.84)	0.94 (0.85)	0.77 (0.56)	1.55 (2.22)	2.37 (1.33)	2.13 (1.09)
Montana (ND)	1.37 (1.33)	1.40 (1.44)	0.47 (0.53)	0.42 (0.61)	0.90 (1.20)	0.98 (1.20)	0.66 (0.69)	0.83 (1.00)

Panel B: Hypothesis tests for equality between Vickrey and Uniform-price formats.^g

	Bid #1	Bid #2	Bid#1-Bid#2	Revenues
Sanders (ND)	t=-1.77 p=0.077	t=2.82 p=0.005	t=-4.09 p=0.000	t=-0.21 p=0.836
Ripken (D)	t=-3.32 p=0.002	t=3.10 p=0.001	t=-6.00 p=0.000	t=-0.38 p=0.702
Jordan (ND)	t=-0.38 p=0.706	t=0.47 p=0.638	t=-0.86 p=0.391	t=-1.42 p=0.156
Montana (D)	t=-0.88 p=0.377	t=1.19 p=0.235	t=-1.52 p=0.128	t=0.44 p=0.658
Montana (ND)	t=-0.08 p=0.937	t=0.34 p=0.733	t=-0.25 p=0.800	t=-0.54 p=0.588

^a Standard deviations of the data are in parentheses.

^b Bid #1 data consists of the first bid submitted by each bidder.

^c Bid #2 data consists of the second bid submitted by each bidder.

^d Bid#1-Bid#2 data consists of the difference between a bidder's first-unit bid and his second-unit bid.

^e Revenue equals the total payment received for both cards in the auction.

^f (ND) denotes a nondealer treatment, while (D) denotes a dealer treatment.

^g We present each t-statistic for the null hypothesis that the Vickrey bid minus the uniform-price bid equals zero, with the corresponding two-tailed p-value.

Table 3. Proportions of zero bids, of flat bid schedules, and of split allocations.

	Zeros on Bid #1 ^a		Zeros on Bid #2 ^b		Flat bid schedules ^c		Split Allocations ^d	
	Vickrey	Uniform	Vickrey	Uniform	Vickrey	Uniform	Vickrey	Uniform
Sanders (ND) ^e	0.0%	0.0%	5.9%	20.6%	14.7%	0.0%	55.9%	85.3%
Ripken (D)	0.0%	0.0%	0.0%	3.3%	36.7%	6.7%	23.3%	86.7%
Jordan (ND)	12.0%	4.0%	34.0%	30.0%	32.0%	22.0%	32.0%	54.0%
Montana (D)	0.0%	0.0%	10.0%	25.0%	20.0%	5.0%	60.0%	45.0%
Montana (ND)	10.0%	13.3%	40.0%	50.0%	30.0%	30.0%	46.7%	53.3%
Overall	5.5%	3.7%	20.1%	26.2%	27.4%	14.0%	41.5%	65.2%

Notes:

- ^a “Zeros on bid #1” indicates the proportion of first-unit bids equal to zero.
- ^b “Zeros on bid #2” is the corresponding proportion for second-unit bids.
- ^c “Flat bid schedules” denotes the proportion of bidders whose bid schedules are flat (first-unit bid equals second-unit bid).
- ^d “Split allocations” indicates the proportion of auctions for which the two goods were split between the two bidders.
- ^e (ND) denotes a nondealer treatment, while (D) denotes a dealer treatment.

Appendix 1. Subject Instructions for Uniform-Price Auction

Welcome to Lister's Auctions. You have the opportunity to bid in an auction for two identical sportscards. There are only two bidders in this auction; the other bidder will be randomly chosen from other participants at today's card show. (If you are a card dealer you will be paired randomly with one other card dealer in your auction. If you are a non-dealer, you will be paired with one other non-dealer.)

The cards up for auction are two copies of the following card: *Card A PSA 8*

Auction Rules:

You are asked to submit two bids — one bid for each card. If you choose to place only one bid, your second bid will be counted as a bid of zero dollars.

Since there are two bidders, there will be a total of four bids submitted. The winning bids will be the highest two from the group of four bids. For each card won, the purchase price is equal to the amount of the third-highest bid (that is, the highest losing bid).

I will order the four bids from highest to lowest in order to determine the winners of the two items.

For example, if the bids are ranked highest to lowest as follows:

\$A
\$B
\$C
\$D

The bidder who bid **\$A** wins one card and pays **\$C**.

The bidder who bid **\$B** wins the second card and pays **\$C**.

Note that one person might have submitted both of the top bids, and thus would buy both cards for **\$C** each.

If a **TIE** occurs between \$B and \$C, I will flip a coin to determine the winner.

Example

Before you submit your actual bids, I would like you to work through an example. Consider a couple of bids that you might submit, and write the numbers here in these two blanks.

my 1st bid _____

my 2nd bid _____

Now make up a couple of bids that the other bidder might submit, and fill those numbers into these blanks.

other bidder's 1st bid _____

other bidder's 2nd bid _____

Take the four bids and order them from highest to lowest:

highest bid: _____ lowest bid: _____

Now, determine how many cards you have won, how many cards the other bidder has won, and the amount each of you has to pay. Fill those numbers in here.

number of cards I won _____ amount I must pay _____

number cards other bidder won _____ amount other bidder must pay _____

To assure that you understand how this auction mechanism operates, I will check your work after you complete this example.

Final Transaction

At 1PM I will determine the winners of each auction completed between 8AM and 12:30PM. For those auctions completed after 1PM I will determine the winners at 5PM. After the winners pay me (cash or check) for the cards, the cards will be awarded to the winners. Note, regardless of price, the cards will be awarded to the winners. In case you cannot attend the “determination of winners” sessions, please provide your name, mailing address, and phone number below:

Name _____

Address _____

Phone# _____

If you are unable to attend at 1PM (or 5PM), I will contact you by phone. Upon receipt of your check or cash, I will send you the cards that you won. All postage will be paid by Lister’s Auctions for cards mailed to winners.

Note that while this is a real auction for real cards, I plan to use data on the bids in this auction for economic research. I guarantee to sell both of the cards listed to the winners of this two-bidder auction, no matter what the final auction prices turn out to be. Your bids represent binding commitments to buy cards you win at the prices specified by the auction outcomes.

Good luck—please write your bids on the sheets provided.

Thanks for participating.

Appendix 2. Subject Instructions for Vickrey Auction

All text is identical to that of Appendix 1, with the exception of the **Auction Rules** shown below:

Auction Rules:

You are asked to submit two bids — one bid for each card. If you choose to place only one bid, your second bid will be counted as a bid of zero dollars.

Since there are two bidders, there will be a total of four bids submitted. The winning bids will be the highest two from the group of four bids. For each card won, the purchase price will be determined as follows.

For the first unit you win, you pay an amount equal to the highest rejected bid which was not your own.

For the second unit you win, you pay an amount equal to the second-highest rejected bid which was not your own.

I will order the four bids from highest to lowest in order to determine the winners of the two items.

Example 1: if the bids are ranked highest to lowest as follows:

\$A (from bidder 1)
\$B (from bidder 2)
\$C (from bidder 2)
\$D (from bidder 1)

Bidder 1 wins one card and pays \$C. Bidder 2 wins the second card and pays \$D.

Example #2. If bids are rank ordered as follows:

\$A (from bidder 1)
\$B (from bidder 1)
\$C (from bidder 2)
\$D (from bidder 2)

Bidder 1 wins one card and pays \$C. Bidder 1 wins the second card and pays \$D.

Example #3. If bids are rank ordered as follows:

\$A (from bidder 1)
\$B (from bidder 2)
\$C (from bidder 1)
\$D (from bidder 2)

Bidder 1 wins one card and pays \$D. Bidder 2 wins the second card and pays \$C.
If a **TIE** occurs between \$B and \$C, I will flip a coin to determine the winner.